

Directions: Be sure to include in-line citations, including page numbers if appropriate, every time you use a text or notes or technology. Include a careful sketch of any graph obtained by technology in solving a problem. **Only write on one side of each page.**

Problems

1. (20 points) Using any previous results, prove part (b) of Proposition 3.21. Given angles $\angle P, \angle Q, \angle R$. If $\angle P < \angle Q$ and $\angle Q \cong \angle R$, then $\angle P < \angle R$.
2. (20 points) Using any previous result, prove the following portion of Proposition 4.4. Every angle has a bisector (do NOT show the bisector is unique.)
3. (20 points each) Do any three (3) of the following.
 - (a) In the following interpretation, all incidence axioms and the first three betweenness axioms hold. Explain why, Proposition 3.4 fails. Use the usual Euclidean model except for three points A, B, P where P is between A and B in the usual Euclidean sense. For these three points re-interpret between to mean “ A is between P and B ”.
 - (b) Using any previous result, prove Proposition 3.20 (Angle Subtraction). Given \overrightarrow{BG} between \overrightarrow{BA} and \overrightarrow{BC} , \overrightarrow{EH} between \overrightarrow{ED} and \overrightarrow{EF} , $\angle CBG \cong \angle FEH$, and $\angle ABC \cong \angle DEF$. Then $\angle GBA \cong \angle HED$.
 - (c) Using any result through Chapter 4 prove the following. Let γ be a circle with center O , and let A and B be two points on γ . The segment AB is called a **chord** of γ . Let M be the midpoint of segment AB . Prove that if $O \neq M$, then the perpendicular bisector of segment AB passes through the center O of γ .
 - (d) Using any result through the corollaries to Theorem 4.3, prove the following.
If $A * B * C$ and $\overleftrightarrow{DC} \perp \overleftrightarrow{AC}$ then $AD > BD > CD$. (See the figure on the board.)