

February 25, 2000

---

Name

Technology used: \_\_\_\_\_

Textbook/Notes used: \_\_\_\_\_

**Directions:** Be sure to include in-line citations, including page numbers if appropriate, every time you use a text or notes or technology. Include a careful sketch of any graph obtained by technology in solving a problem. **Only write on one side of each page.**

**The Problems**

1. Use the definition (the limit form) of derivative to find  $f'(x)$  if  $f(x) = \frac{1}{2x+1}$ .
2. Below is the graph of a function on a grid. Assuming the grid lines are spaces 1 unit apart both vertically and horizontally, sketch the graph of the derivative function over the same interval. Use the same

grid for your sketch.

3. State the definition of:

- (a) A function  $f$  being continuous at  $x = c$ .
- (b) A function  $f$  being differentiable at  $x = c$ .

4. Given the function  $f(x) = \begin{cases} x^2 - 6, & x < 2 \\ -2, & x = 2 \\ Ax - 12, & x > 2 \end{cases}$

- (a) Determine, with explanation, a value of  $A$  that makes  $f$  continuous at  $x = 2$  or explain why no such number  $A$  exists.

5. Do **one** of the following.

- (a) When working with the exponential function  $f(x) = 3^x$ , some people prefer to use the function  $g(x) = e^{kx}$  where  $k = \ln(3)$ . Use logarithm and exponential rules to show these are really the same function.
- (b) Determine the **exact** values of each of the following.
- $\arcsin(1)$
  - $\arctan(1)$
  - $\cos(\arccos(\sqrt{2}/2))$
  - $\arcsin(\sin(12\pi))$  [Be careful.]
  - $\exp(3 \ln(4))$ .

6. Do **one** of the following.

- (a) Without using a calculator, determine the following limits. Be sure to briefly justify your answer.
- 

$$\lim_{x \rightarrow 0} \frac{\sin^2(x)}{x}$$

ii.

$$\lim_{x \rightarrow 0} \frac{1}{1 + 3^x}$$

iii.

$$\lim_{x \rightarrow 2} \frac{x^2 + 5x - 14}{3x^2 - 3x - 6}$$

- (b) Without using a calculator, determine the following limits. Be sure to justify your answer.
- 

$$\lim_{x \rightarrow 1^-} \frac{10}{1 + 2^{1/(x-1)}}$$

ii.

$$\lim_{x \rightarrow 0^+} \left( \frac{1}{x} - \frac{1}{x^2} \right) \quad \text{Hint: } \frac{\infty}{\infty} \text{ is a "be careful" (indeterminate) form.}$$