1 Mathematics 433

November 10, 2000

Name

Directions: Be sure to include in-line citations, including page numbers if appropriate, every time you use the results of discussion, a text, notes, or technology. **Only write on one side of each page.**

"'Know thyself?' If I knew myself, I'd run away." - Johann von Goethe

Problems

- 1. Prove the icosahedral group has no subgroup of order 30.
- 2. Prove no group of order p^l , where p is prime and l > 1, is simple.
- 3. List all subgroups of the dihedral group D_4 , and divide them into conjugacy classes.
- 4. Do **both** of the following.
 - (a) Let H be a normal subgroup of a group G of order 2. Prove H is in the center of G.
 - (b) Let H be a normal subgroup of prime order p in a finite group G. Suppose p is the smallest prime dividing |G|. Prove H is in the center of G.
- 5. Prove no group of order p^2q , where p and q are distinct primes, is simple.
- 6. Do **one** of the following.
 - (a) Prove the only simple groups of order less than 60 are groups of prime order.
 - (b) Classify all groups of order 33.
 - (c) Classify all groups of order 18.