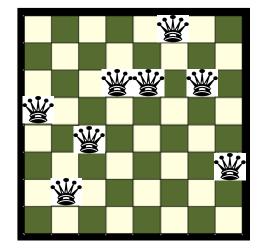


Today

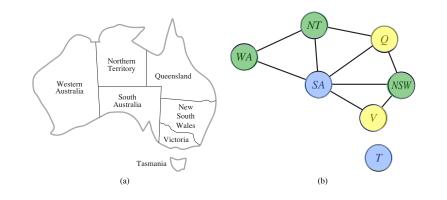
- Local Search Algorithms
 - Simulated Annealing
 - Genetic algorithms
 - Gradient ascent

The N-Queens problem

complete state formulation



Map Colorings



Local Search Algorithms

The basic idea:

- 1. Randomly initialize state
- 2. If not goal state,
 - a. make local modification to generate neighbor state OR
 - b. enumerate all neighbor states and choose the best
- 3. Repeat step 2 until goal state is found (or out of time)
- □ Requires the ability to quickly:
 - Generate a random (probably-not-optimal) state
 - Evaluate the quality of a state
 - Move to other states (well-defined neighborhood function)

Local Search Algorithms

- □ Use when path to goal is irrelevant
- Minimal memory requirements keep track of current state only
- Algorithms include:
 - Hill-climbing
 - Simulated annealing
 - Local beam search
 - Genetic algorithms
 - Gradient descent (Newton-Rhapson)

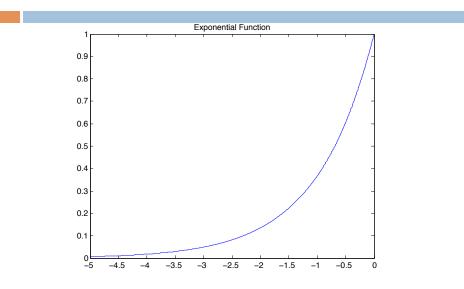
Local Search Terminology

Simulated Annealing

- □ Proposed in 1983
- □ Borrows from the idea of annealing in physics
 - Liquid cools too quickly, atoms solidify into sub-optimal configuration (local minimum)
 - Liquid cools slowly, atoms solidify into minimum energy configuration (global minimum)
- Early applications
 - Design of electronic systems
 - Traveling salesman

Simulated Annealing

Simulated Annealing



Genetic Algorithms

Survival of the fittest!

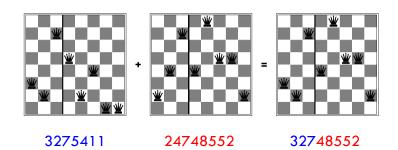
- Initialize population to N randomly generated states represented as strings over finite alphabet
- Evaluate the fitness of each individual via fitness function (higher=better)
- □ To generate a new population, repeat:
 - Randomly select 2 individuals proportional to their fitness
 - Randomly pick a crossover point and produce 2 new children
 - Randomly mutate each location of the new children

Genetic Algorithms

24748552	24 31%	32752411	32748552	► 32748152
32752411	23 29%	24748552	24752411	► 24752411
24415124	20 26%	32752411	32752124	► 32 <mark>2</mark> 52124
32543213	11 14%	24415124	24415411	► 2441541 <mark>7</mark>
(a)	(Ъ)	(c)	(d)	(e)
Initial Population	Fitness Function	Selection	Cross-Over	Mutation

- □ Fitness function: number of non-attacking pairs of queens
- \Box 24/(24+23+20+11) = 31%
- \square 23/(24+23+20+11) = 29% etc

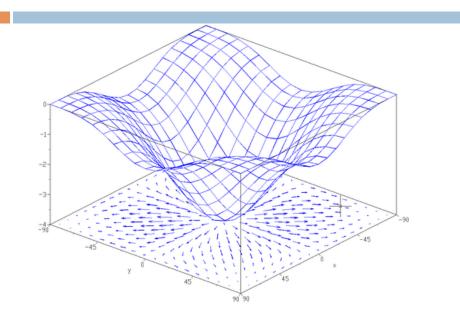
Genetic Algorithms



Genetic Algorithms

- Contiguous blocks of string representation must correspond to some meaningful information!
- Developing a string rep., crossover, and mutation function not always straightforward (e.g. TSP – give it a try!)
- Crossover can produce an offspring that is in an entirely different area of the search space than either parent
 - Sometimes offspring is outside of the "feasible" or "evaluable" region

Gradient-based methods



Gradient-based methods

"Their operation is similar to a blind man walking up a hill, whose only knowledge of the hill comes from what passes under his feet. If the hill is predictable in some fashion, he will reach the top, but it is easy to imagine confounding terrain"

- Goffe et al., 1994

Gradient-based methods

- □ Gradient-based methods
 - Continuous function
 - First derivative easily computable
- □ Newton-Rhapson for optimization
 - Requires computing the first- and second-derivative
- □ Gradient ascent/descent
 - The poor man's version of NR

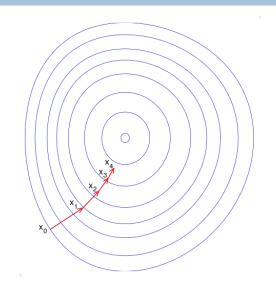
Newton-Rhapson

Newton-Rhapson for optimization

Gradient Ascent (Descent)

function GRADIENT-ASCENT(F, γ) returns solution $\nabla F \leftarrow \text{COMPUTE-GRADIENT}(F)$ $x \leftarrow \text{a randomly selected value}$ while stopping criteria $x \leftarrow x + \gamma \nabla F(x)$ return x

Gradient Ascent (Descent)



Local search summary

- □ Hill-climbing search
 - Stochastic hill-climbing search
 - First-choice
 - Random restart hill-climbing
- Local beam search
 - Stochastic local beam search
- Simulated Annealing
- □ Genetic algorithms
- □ Gradient-based methods
 - Newton-Rhapson
 - Gradient ascent (descent)

Read on your own!