

SL: PUTTING IT ALL TOGETHER

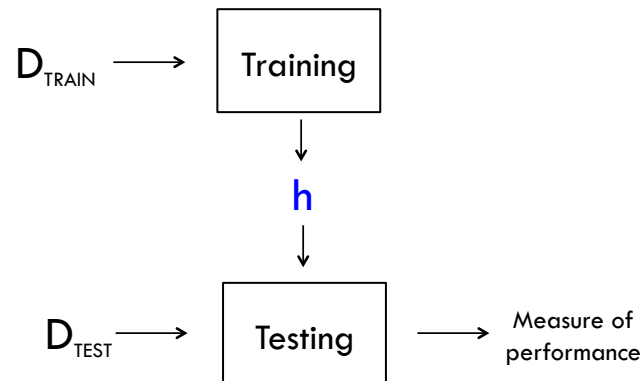
Today

- Goals
 - Step 1: Formulating the problem
 - Step 2: Exploring the data
 - Step 3: Feature Selection
 - Step 4: Training
 - Step 5: Testing

The first 4 steps are not necessarily done in a strict linear progression

Overview

$$D = \{(\mathbf{x}_i, y_i) \mid i = 1, \dots, N\} \quad \text{where} \quad f(\mathbf{x}_i) = y_i$$



Step 1: Formulate the problem

- What quantity are you predicting?
 - ▣ real-valued, categorical, structure?
 - ▣ Changing over time?
 - ▣ Classification
 - Binary classification? Multi-class classification?
 - Singly-labeled? Multi-labeled?
 - For multi-labeled classification tasks, how correlated are the labels?

Step 1: Formulate the problem

- What data do you have?
 - ▣ Where to get labeled data? (Amazon mechanical turk)
 - ▣ How much labeled data?
 - ▣ What is the quality of the labeled data?
 - ▣ Are the labels learnable given the data?
 - ▣ Is the distribution of labels in the data skewed/
imbalanced?

Guiding Principles

- Unsupervised learning as a surrogate for supervised learning...is a headache. Just get the labels.
- Reproducibility
- Think of how you would justify each decision you made
- Start simple and iterate

Reducing multi-class to binary task

One-vs-All	original training data	c1 vs. all	c2 vs. all	c3 vs. all																																
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One-vs-One	original training data	c1 vs. c2	c1 vs. c3	c2 vs. c3																																
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Multi-label Classification

- Each example can be labeled with multiple labels
 - ▣ Don't confuse this with multi-class classification!
 - ▣ Common for document classification or object recognition
- One-vs-all
- One classifier for every possible combination of labels
 - ▣ Combinatorial explosion
 - ▣ Limited training data



Step 2: Exploratory Data Analysis

- Look at the data. It's surprising how often we forget to actually do this!
- **Exploratory Data Analysis** (EDA) is a statistical mindset
 - Box plots, histograms, scatter plots, mean, mode, deviations
 - Can guide the modeling process by
 - give you insight into the data
 - help (in)validate your assumptions
 - detect outliers

Step 3: Feature Selection

- What features should I use?
 - Dimensionality reduction if exist time/space constraints
 - Reduce noise in the data (irrelevant or redundant features)
- Dimensionality reduction
 - Principal component analysis (PCA)
 - Singular value decomposition (SVD)
 - Canonical correlation analysis (CCA)
- Regularization
 - Use every feature but penalize classifiers that are overly complex

$$\text{Error}(w) = \sum_{i=1}^N (y_i - h_w(x_i)) + \lambda \|w\|^2$$

encourages sparse weight vectors

Other tricks

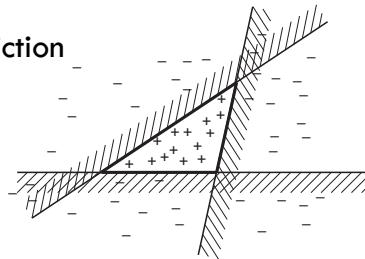
- Scale input features
- Transform features
 - e.g., take log
- Higher-order features
 - e.g., product of features
- Again, EDA can help guide this process

Step 4: Training

- Pick your classifier
 - Decision tree, perceptron, neural network, SVM, linear regression, logistic regression, random forests, ensembles, Gaussian process regression, hidden Markov models, conditional random field, Bayesian networks,...
 - Bagging or Boosting
- Your choice is informed by all of the previous steps
- Often there are parameters that must be tuned...

Ensembles of Classifiers

- An ensemble of classifiers – A group of classifiers whose predictions are combined to produce one final prediction
- Benefits
 - ▣ Harder to make a wrong prediction
 - ▣ More expressive hypothesis



Boosting

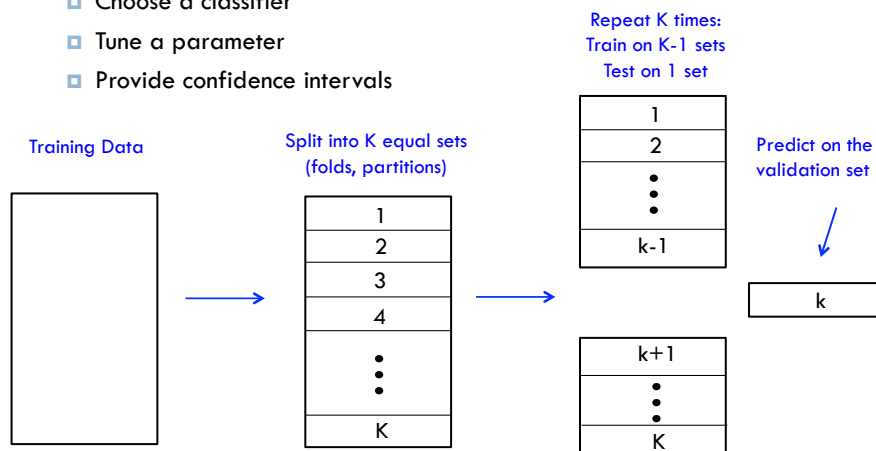
- Learn a series of **weak classifiers**
- Weight each weak classifier to create a final strong classifier
- Often the weight for each classifier is proportional to its accuracy
- **AdaBoost** (Freund and Schapire 1995)

Bagging

- Short for “Bootstrap aggregating”
- Given training set D
 - ▣ Generate M new training sets D_i where $|D_i| < |D|$ by sampling from D with replacement
 - ▣ This is a statistical technique known as **bootstrapping**
 - ▣ Train a classifier on each of the M new training sets
 - ▣ Combine output of M classifiers using averaging or voting
- Random Forests (Breimen, 2001)
 - ▣ Bagged decision trees

Cross Validation

- K-fold cross validation
 - ▣ Choose a classifier
 - ▣ Tune a parameter
 - ▣ Provide confidence intervals



Step 5: Testing

- We have a final hypothesis
- We now use our hypothesis to predict on new (unseen) examples from the test set.
 - ▣ There's no going back and tweaking the classifier based on its test set performance!

Binary Classification: Measures of Performance

- The contingency table is given by:

	$y = 1$	$y = 0$
$h = 1$	TP	FP
$h = 0$	FN	TN

- ▣ TP is the number of *true positives*
- ▣ FP is the number of *false positives*
- ▣ FN is the number of *false negatives*
- ▣ TN is the number of *true negatives*

Binary Classification: Measures of Performance

$$\text{Accuracy} = \frac{TP + TN}{TP + FP + TN + FN}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$

$$F_1\text{-score} = 2 \cdot \frac{\text{Prec} \cdot \text{Recall}}{\text{Prec} + \text{Recall}}$$

	y = 1	y = 0
h = 1	TP	FP
h = 0	FN	TN

Contingency Table

Binary Classification: Measures of Performance

$$\text{Accuracy} = \frac{7 + 8}{7 + 8 + 2 + 3} = \frac{15}{20} = .75$$

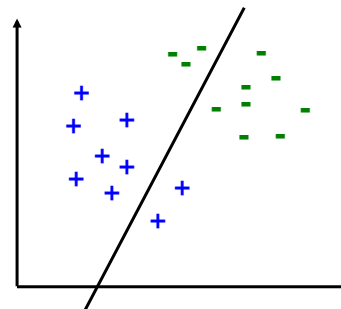
$$\text{Precision} = \frac{7}{7 + 3} = .70$$

$$\text{Recall} = \frac{7}{7 + 2} = .78$$

$$F_1\text{-score} = 2 \left(\frac{.70 \cdot .78}{.70 + .78} \right) = 2 \left(\frac{.546}{1.48} \right) = .74$$

	y = 1	y = 0
h = 1	7	3
h = 0	2	8

Contingency Table



Multi-class Classification: Measures of performance

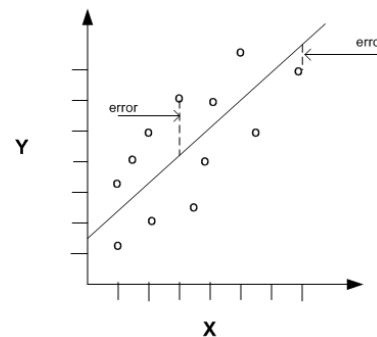
- Evaluate each label separately using a “one-vs-all” approach
 - Macro-averaging
 - Compute the measure (precision, recall, F_1) for each class
 - Average across all C classes
 - Gives equal weight to all classes
 - Micro-averaging
 - Pool the TP, FP, FN, TN for all C classes
 - Compute the measure (precision, recall, F_1)
 - Weighted towards performance of most likely class

	$y_c = 1$	$y_c = 0$
$h_c = 1$	TP_c	FP_c
$h_c = 0$	FN_c	TN_c

Contingency Table

Regression: Measures of performance

- Mean-squared error
- Root mean-squared error
- Mean absolute error
- Mean absolute percentage
- ...



Summary

- Overview
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