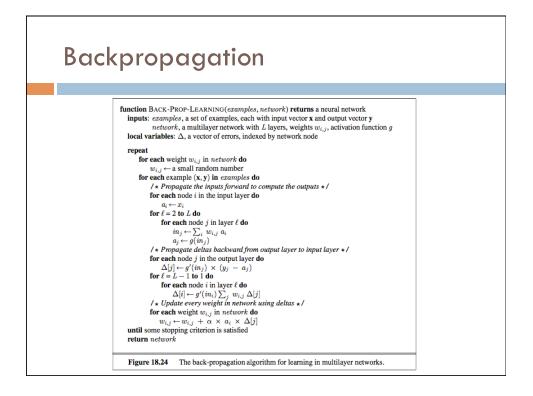
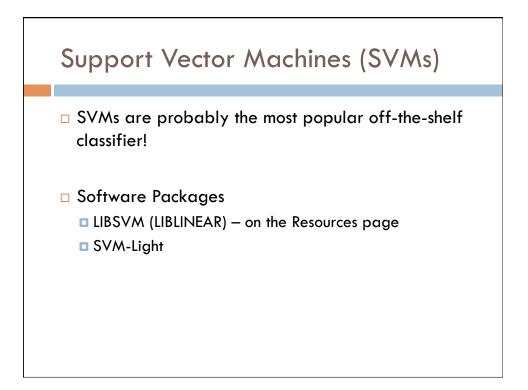


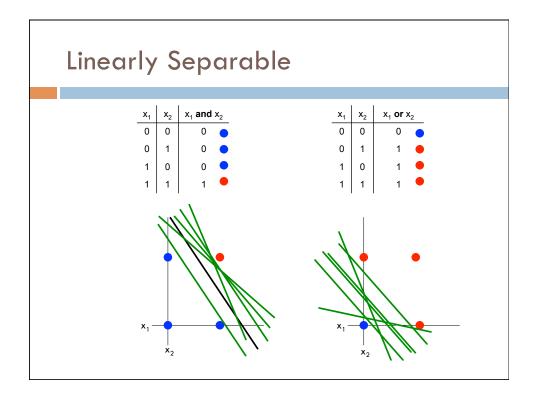
Backpropagation

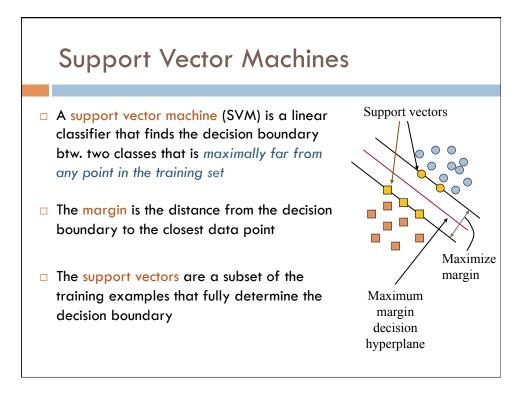
- 1. Begin with randomly initialized weights
- 2. Apply the neural network to each training example (each pass through examples is called an epoch)
- 3. If it misclassifies an example modify the weights
- Continue until the neural network classifies all training examples correctly

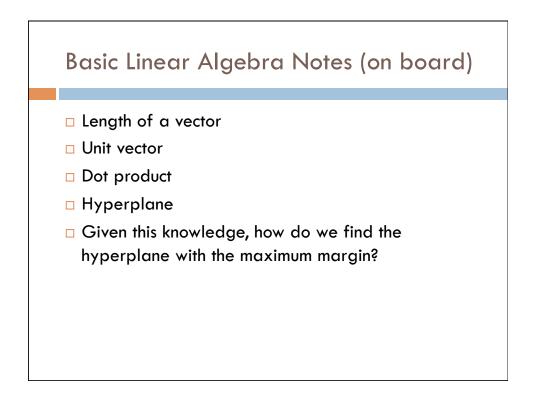
(Derive gradient-descent update rule)







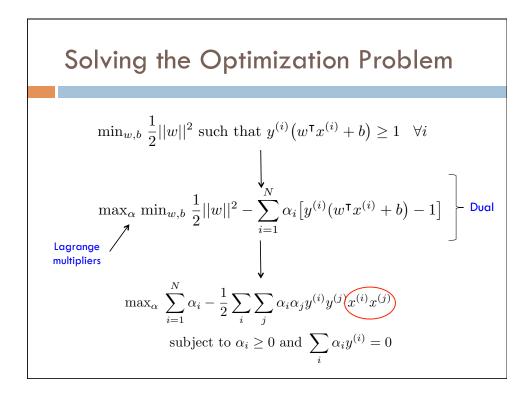




Solving the Optimization Problem

 $\min_{w,b} \frac{1}{2} ||w||^2 \text{ such that } y^{(i)} \left(w^{\mathsf{T}} x^{(i)} + b \right) \ge 1 \quad \forall i$

- Need to optimize a quadratic function subject to linear constraints
- Quadratic optimization problems are a well-known class of mathematical programming problem and many algorithms exist for solving them
- The solution involves constructing a dual problem where a Lagrange multiplier (a scalar value) is associated with every constraint in the primary problem

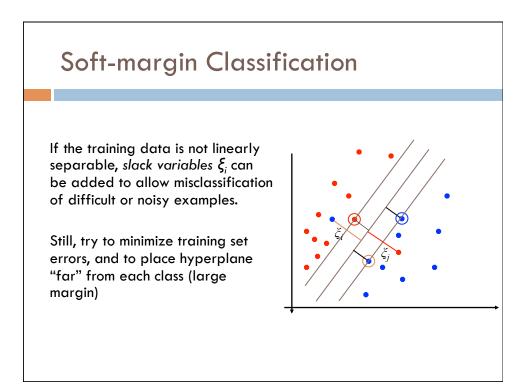


Solving the Optimization Problem

The solution has the form:

$$w = \sum_{i=1}^{N} \alpha_i y^{(i)} x^{(i)}$$
 and $b = y^{(i)} - w^{\mathsf{T}} x^{(i)}$ for any $x^{(i)}$ s.t. $\alpha_i \neq 0$

- $\hfill\square$ Each non-zero alpha indicates corresponding x_i is a support vector
- □ The classifying function has the form: $g(x_i) = sign\left(\sum_i \alpha_i y^{(i)} x^{(i)} x + b\right)$
- Relies on an inner product between the test point x and the support vectors x_i



How many support vectors?

- Determined by alphas in optimization
- Typically only a small proportion of the training data
- The number of support vectors determines the run time for prediction

How fast are SVMs?

Training

- Time for training is dominated by the time for solving the underlying quadratic programming problem
- Slower than Naïve Bayes
- Non-linear SVMs are worse

Testing (Prediction)

- Fast - as long as we don't have too many support vectors

