

AGENTS AND ENVIRONMENTS

What is AI in reality?

- “AI is our attempt to create a ‘machine’ that thinks (or acts) humanly (or rationally)”

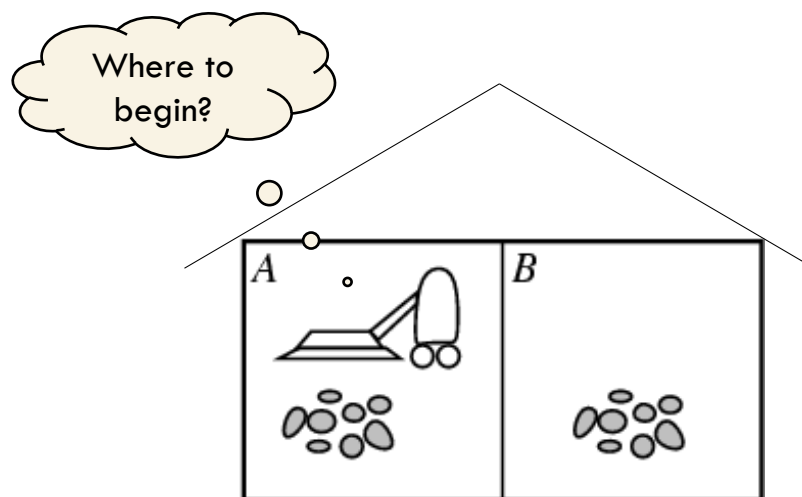
Think like a human Cognitive Modeling	Think rationally Logic-based Systems
Act like a human Turing Test	Act rationally Rational Agents

Today

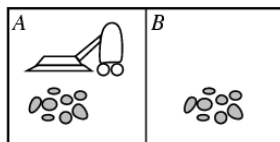
- Reading
 - ▣ Artificial Intelligence: A modern approach (AIMA)
Section 2.1-2.3, 3.1

- Goals
 - ▣ Rational agents
 - ▣ Task environment
 - ▣ Uninformed search

How do we create an intelligent vacuum?

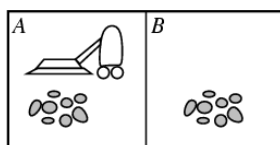


Agents



- An **agent** is any thing that **perceives** the world through sensors and **acts** on the world through actuators.

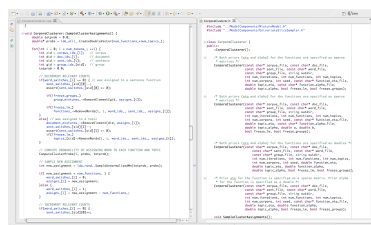
Agents



- An **agent** is any thing that **perceives** the world through sensors and **acts** on the world through actuators.
- percepts - which room, dirt in the room
- actions - Left, Right, Suck, Do Nothing

Agents

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Agents

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What is rationality?

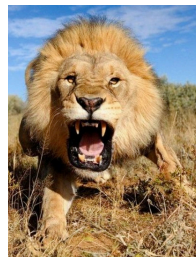


Sing a song
Run
Smile
Run and scream

So what makes an agent rational?

Rational agents

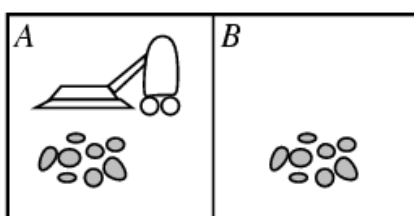
- For each percept sequence, a **rational** agent chooses an action that maximizes its **performance measure** given evidence from percept (sequence) and **prior knowledge**



~~**Sing a song**~~
Run
Smile
Run and scream

Rational agents

- For each percept sequence, a **rational** agent chooses an action that maximizes its **performance measure** given evidence from percept (sequence) and **prior knowledge**



Characterizing the task environment

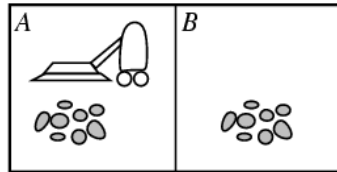
- Now that we've defined a rational agent we want to specify the sort of environment in which that agent operates:
 - fully-observable, partially observable, unobservable
 - single agent vs. multi-agent
 - deterministic vs. stochastic
 - discrete vs. continuous

Solving problems by Searching

Search

- We have an rational agent. But how does the agent actually achieve its goal?
- Search for a **solution** - a sequence of actions that leads from the initial state to the goal state
- Uninformed search algorithms
 - ▣ Uses no information beyond problem
 - ▣ Discrete environment
 - ▣ Offline exploration

Formulating the search problem

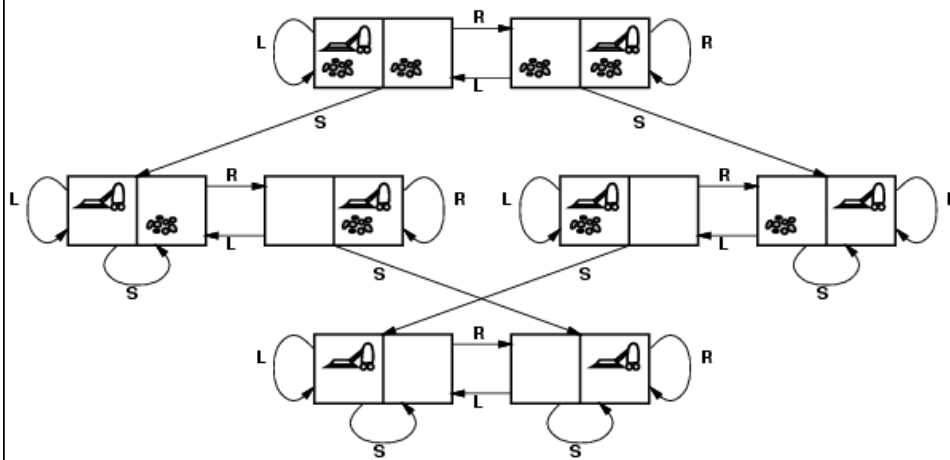


A well-defined search **problem** includes:

- states
 - initial state
 - actions/successor function
 - goal test
 - path cost (reflects performance measure)
- } called the **state space**

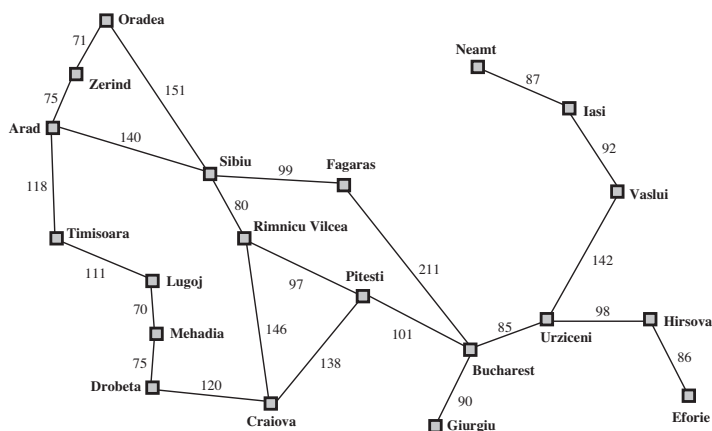
State space graph

The state space induces a graph structure:



Example: Path to Bucharest

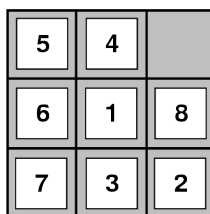
- states?
- initial state?
- actions?
- goal test?
- path cost?



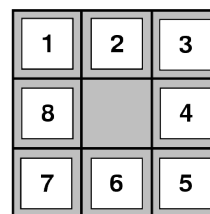
The map of Bucharest is also the state-space graph

Example: 8-puzzle

- states?
- initial state?
- actions?
- goal test?
- path cost?
- What does the state space look like?



Start State

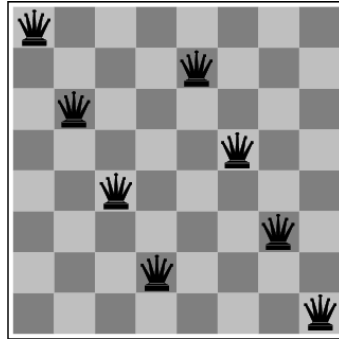


Goal State

states – all possible configurations of the 8 tiles and the blank space
 actions – move the blank space UP, DOWN, LEFT, RIGHT
 path cost – a cost of 1 per action

Example: 8-queens puzzle

- states?
- initial state?
- actions?
- goal test?
- path cost?
- What does the state space look like?

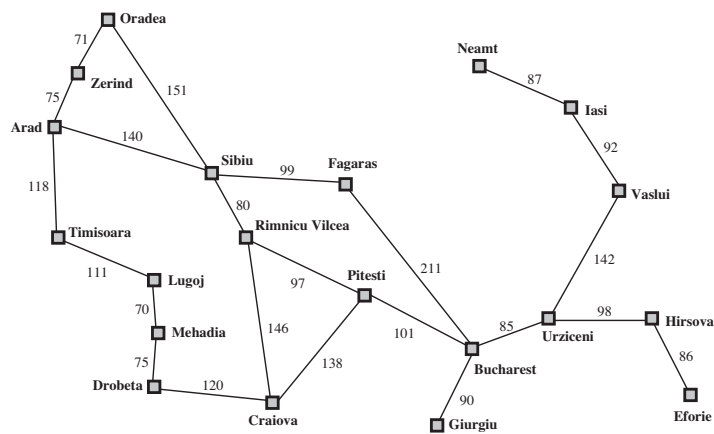


incremental formulation: Initial state is a blank board. An action is to place a queen in the leftmost empty column (such that it is not in conflict with any previously placed queens)

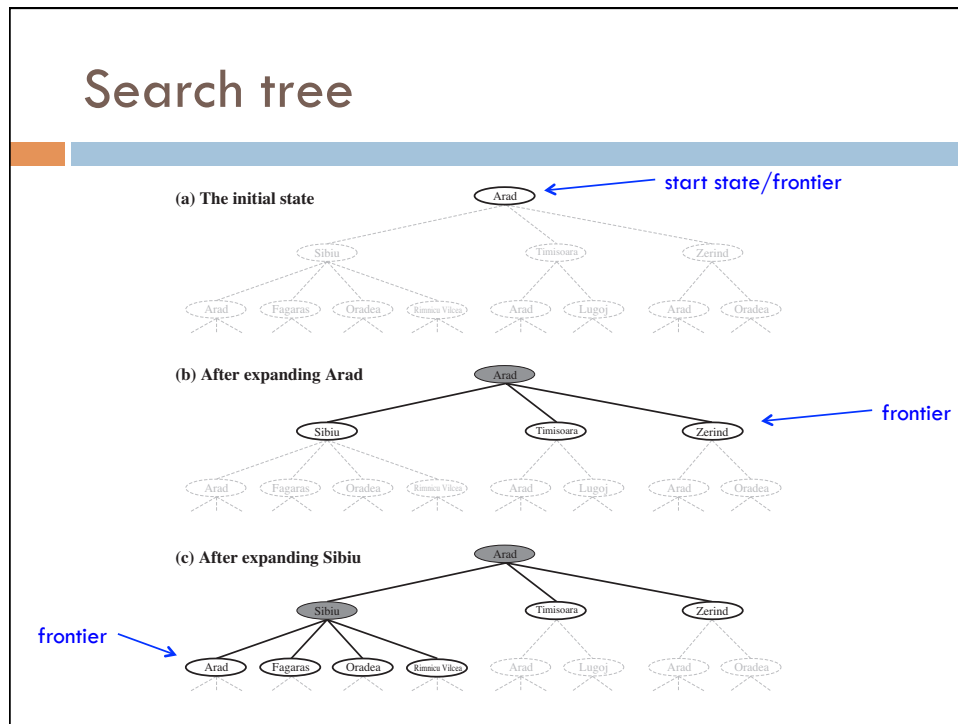
Complete-state formulation: Initial state is 8 queens on the board. An action is to move a queen.

Note the path cost is irrelevant. We care only about the final configuration.

Example: path to Bucharest



Search tree

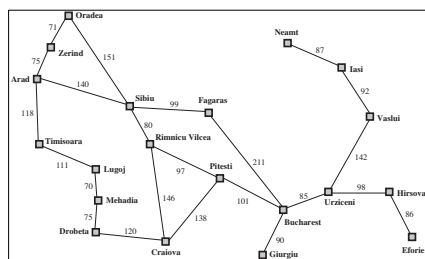


Tree-search algorithm

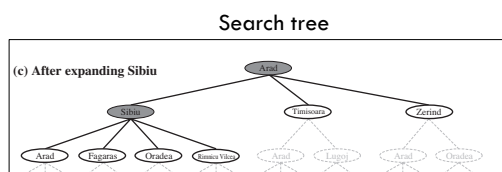
```

function TREE-SEARCH(problem, strategy) returns a solution or failure
  initialize the frontier using the initial state of problem
  loop do
    if the frontier is empty return failure
    choose node according to strategy and remove from frontier
    if node contains goal state return solution
    expand chosen node and add resulting nodes to frontier
  
```

State space graph vs. Search tree



State space graph



Careful! States versus nodes

- A **state** is a symbolic representation
- A **node** is a data structure
- Multiple nodes can point to the same state
- Keep an explored list which stores already-visited nodes

Graph-search

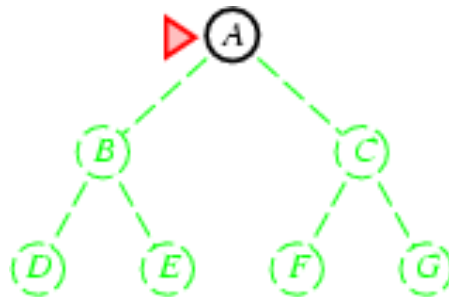
```
function GRAPH-SEARCH(problem, strategy) returns a solution or failure
  initialize the frontier using the initial state of problem
  initialize explored set to empty
  loop do
    if the frontier is empty return failure
    choose leaf node according to strategy and remove from frontier
    if node contains goal state return solution
    add node to explored set
    expand chosen node and add resulting nodes to frontier
    only if not in frontier or explored set
```

Search Strategies

A **search strategy** specifies the order in which nodes are selected from the frontier to be expanded

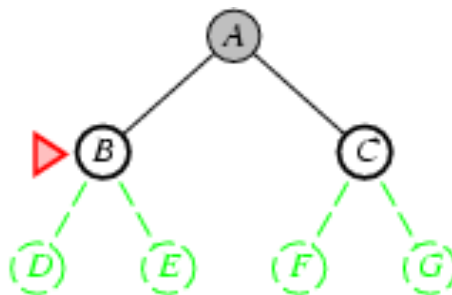
Breadth-first search (BFS)

- Expand shallowest unexpanded node
- **Implementation:**
 - *frontier* is a FIFO queue, i.e. new successors go at end



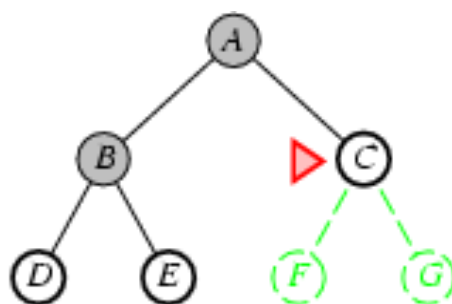
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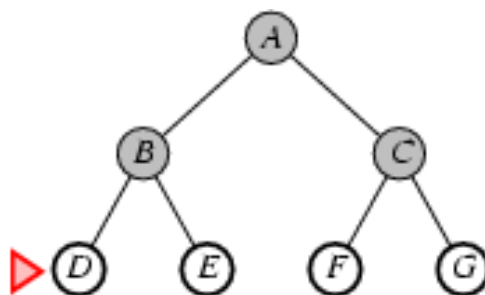
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Evaluating search algorithm

- Time (Big-O)
 - ▣ approximately the number of nodes generated (frontier plus explored list)
- Space (Big-O)
 - ▣ the max # of nodes stored in memory at any time
- Complete (yes/no)
 - ▣ If a solution exists, will we find it?
- Optimal (yes/no)
 - ▣ If we return a solution, will it be the best/optimal solution, i.e. solution with lowest path cost

Evaluating search algorithm

- When analyzing time and space, often use quantities
 - ▣ b – branching factor, i.e. max number of successors of any node
 - ▣ d – depth of the shallowest goal node
 - ▣ m – maximum possible depth of search tree
- Analyze BFS: time, space, completeness, optimality

Analyzing BFS

- Time: $O(b^d)$
- Space: $O(b^d)$
- Complete = YES if branching factor is finite
- Optimal = YES if path cost is non-decreasing function of depth of the node
- (Useful if step costs are constant)

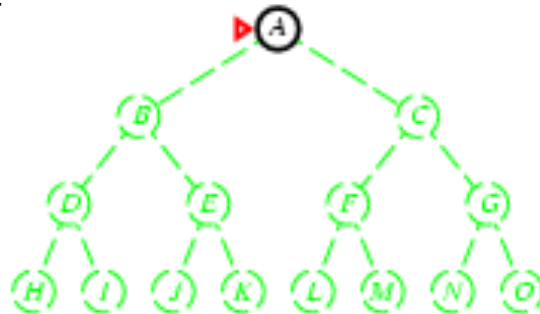
Time and memory requirements for BFS

Depth	Nodes	Time	Memory
2	1100	.11 sec	1 MB
4	111,100	11 sec	106 MB
6	10^7	19 min	10 GB
8	10^9	31 hours	1 terabyte
10	10^{11}	129 days	101 terabytes
12	10^{13}	35 years	10 petabytes
14	10^{15}	3,523 years	1 exabyte

BFS with $b=10$; 10,000 nodes/sec; 10 bytes/node

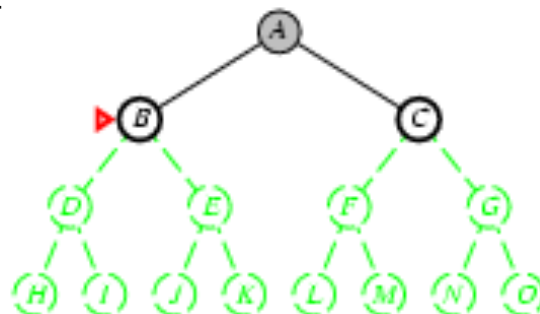
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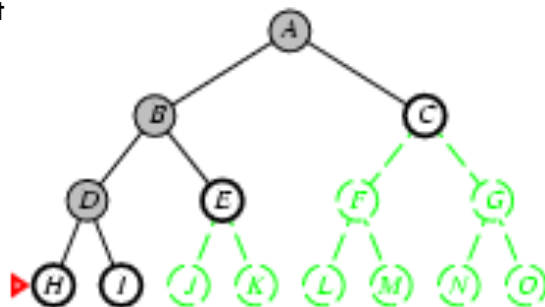
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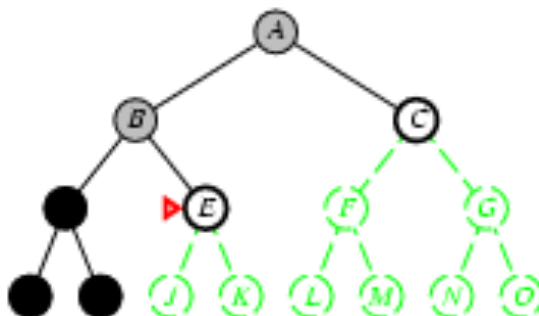
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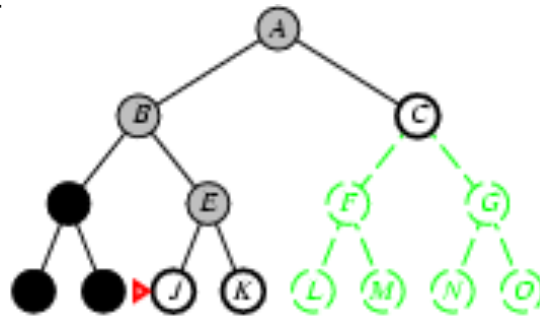
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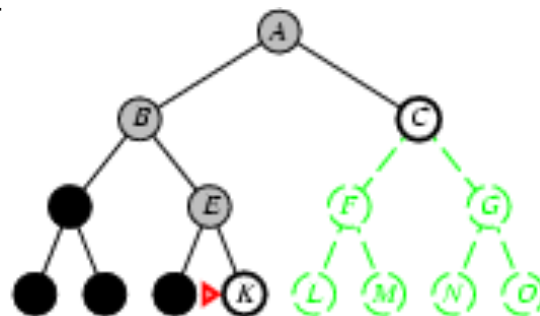
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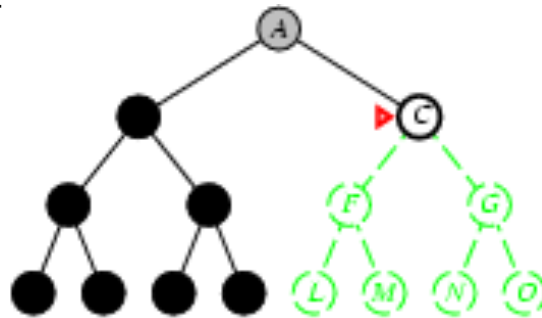
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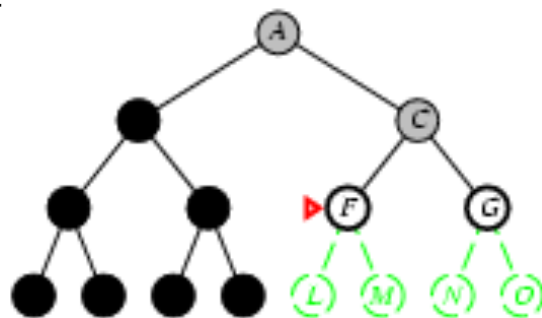
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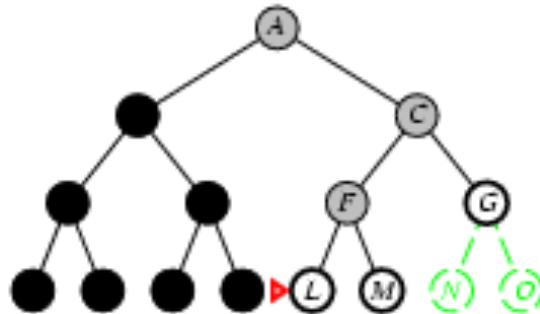
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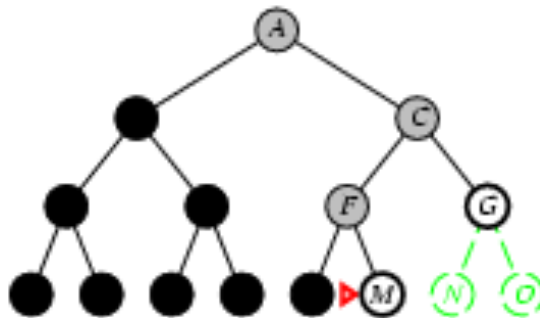
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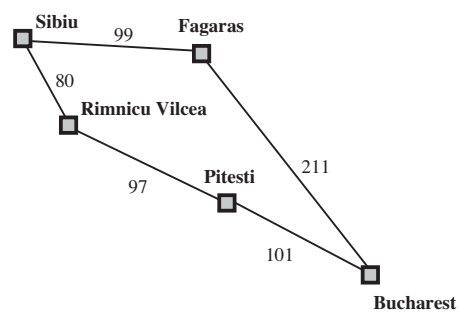


Analyzing DFS

- Time: $O(b^m)$
- Space: $O(bm)$
- Complete = YES, if space is finite (and no circular paths), NO otherwise
- Optimal = NO

Uniform-cost search

- Expand node with lowest path cost
- **Implementation:**
 - *frontier* is a priority queue ordered by path cost



Analyzing Uniform-cost search

- Time: $O(b^{C^*/\epsilon})$
- Space: $O(b^{C^*/\epsilon})$
- Complete = YES if step cost exceeds epsilon
- Optimal = YES

BFS versus DFS

	Time	Space	Complete	Optimal
BFS	$O(b^d)$	$O(b^d)$	Yes	Yes
DFS	$O(b^m)$	$O(b^m)$	Yes	No

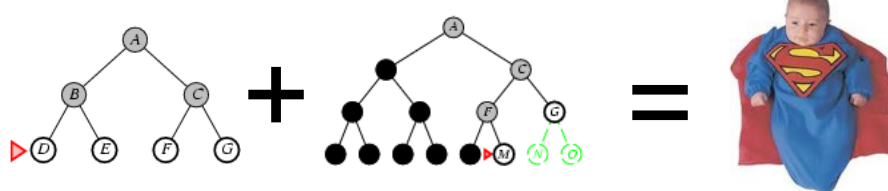
- Which strategy would you use and why?
- Brainstorm improvements to DFS and BFS

Problems with BFS and DFS

- BFS
 - ▣ memory! ☹️
- DFS
 - ▣ Not optimal
 - ▣ And not even necessarily complete!

Improvements?

- Can we combined the optimality and completeness of BFS with the memory of DFS?



Depth limited DFS

- DFS, but with a depth limit **L** specified
 - ▣ Nodes at depth **L** are treated as if they have no successors
 - ▣ We only search down to depth **L**
- Time?
 - ▣ $O(b^L)$
- Space?
 - ▣ $O(bL)$
- Complete?
 - ▣ No, if solution is longer than **L**
- Optimal
 - ▣ No, for same reasons DFS isn't

Iterative deepening search (IDS)

```

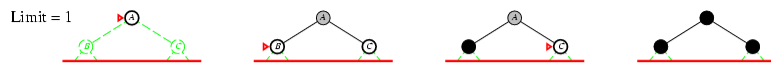
for depth=0, 1, 2, ...
  run depth-limited DFS
  if solution found return result
  
```

- Blends the benefits of BFS and DFS
 - ▣ searches in a similar order to BFS
 - ▣ but has the memory requirements of DFS
- Will find the solution when **L** is the depth of the shallowest goal

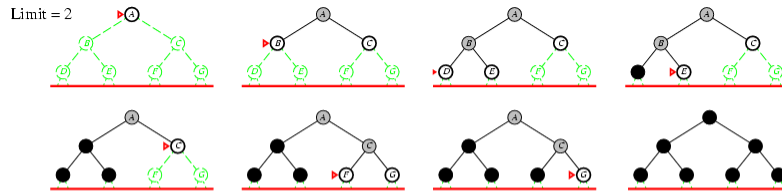
Iterative deepening search $L = 0$



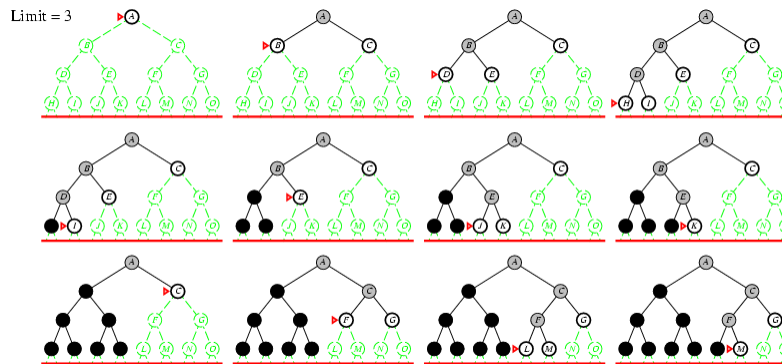
Iterative deepening search $L = 1$



Iterative deepening search $L = 2$



Iterative deepening search $L = 3$



Time complexity for IDS

- $L = 0: 1$
- $L = 1: 1 + b$
- $L = 2: 1 + b + b^2$
- $L = 3: 1 + b + b^2 + b^3$
- ...
- $L = d: 1 + b + b^2 + b^3 + \dots + b^d$
- Overall:
 - ▣ $d(1) + (d-1)b + (d-2)b^2 + (d-3)b^3 + \dots + b^d$
 - ▣ $O(b^d)$
 - ▣ Cost of the repeat of the lower levels is subsumed by the cost at the highest level

Analysis of IDS

- Space
 - ▣ $O(bd)$
- Complete?
 - ▣ Yes
- Optimal?
 - ▣ Yes